

## INTRODUCTION

In DVB-S2, the demodulation is done in four steps which are successively : time synchronization followed by frequency synchronization, phase correction and the generation of the Log Likelihood Ratio (LLR) of the transmitted bits [1]. In [2], we presented a synchronization method using polar coordinates. In this paper, we present the extension of the polar representation to the LLR generation of 8-PSK modulation. The exact computation of the LLR is given by:

$$L^i(b) = \log \frac{\sum_{c \in C_i^0} e^{-\frac{(c-y)^2}{2\sigma^2}}}{\sum_{c \in C_i^1} e^{-\frac{(c-y)^2}{2\sigma^2}}} \quad (1)$$

where  $C_i^0$  (respectively  $C_i^1$ ) is the subset of the points of the constellation so that the  $i$ th bit,  $i \in 0, 1, 2$  is equal to  $b_i = 0$  (respectively,  $b_i = 1$ ),  $y$  is the received point from the channel and  $\sigma^2$  is the variance of the noise. We propose to approximate (1) in the polar domain by using the module  $\rho$  and the phase  $\theta$  of the received point.

Figure 1 presents the steps of the quantification process. From an  $y$  received, an optimal  $\tilde{L}^i$  is computed from its exact and quantified polar coordinates. We propose to compute an approximate LLR ( $\tilde{L}^i$ ) from quantified polar coordinates.

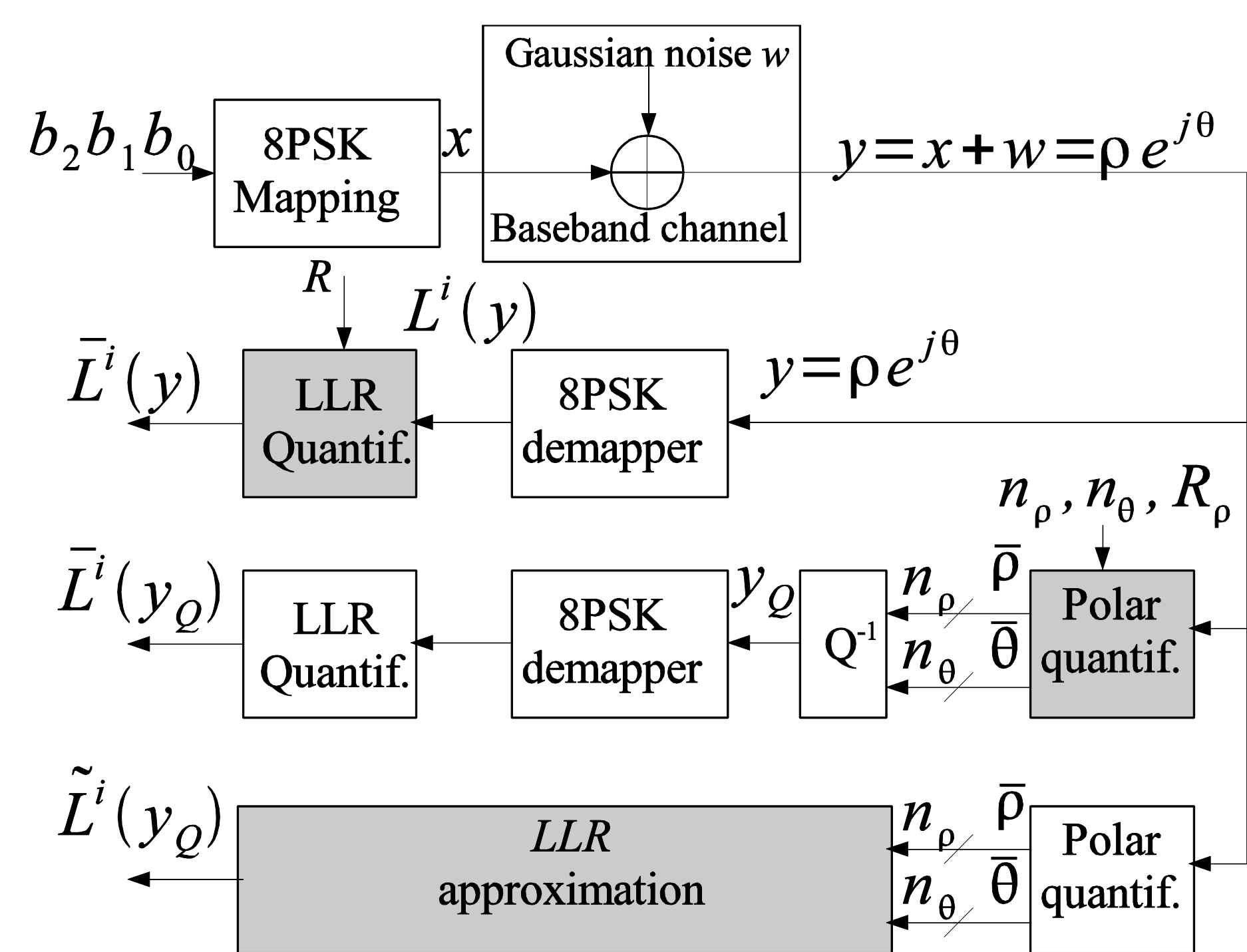


Figure 1 : The 3 steps of the quantization process

## MATERIALS AND METHODS

### APPROXIMATION OF LLR COMPUTATION

Figure 2 shows the quantified value of  $\tilde{L}_{i=0,1,2}^i(y_q)$  on 5 bits computed in figure 1. It has a very regular periodic triangular shape that can be easily interpolated. We can see that it can be approximated by a piecewise linear function. To avoid the direct computation of the LLRs, we propose to compute it with :

$$\tilde{L}^i = \lfloor s_i(\bar{\theta}) \min((\bar{\rho} \min(h_i(\bar{\theta}), 30)\alpha_i) + 0.5, 15) \rfloor$$

Where  $s_i(\bar{\theta})$  is a function that defines the sign of the LLR,  $h_i(\bar{\theta})$  performs translation and/or symmetry on  $\bar{\theta}$  and  $\alpha_i$  is a scaling factor that depends on the LDPC code rate. Figure 3 shows the steps of the quantization process to compute  $\tilde{L}^0$ . The same architecture will be conceived to compute  $\tilde{L}^1$  and  $\tilde{L}^2$ . Since  $\alpha_0 = \alpha_1$ , only one multiplier is required to obtain  $\bar{\rho}\alpha_0$  and  $\bar{\rho}\alpha_1$ . We also know that  $s_i(\bar{\theta}) = \pm 1$ , then no multiplier is required for this step. To calculate  $\tilde{L}$  for a whole symbol, 5 multipliers should be implemented.

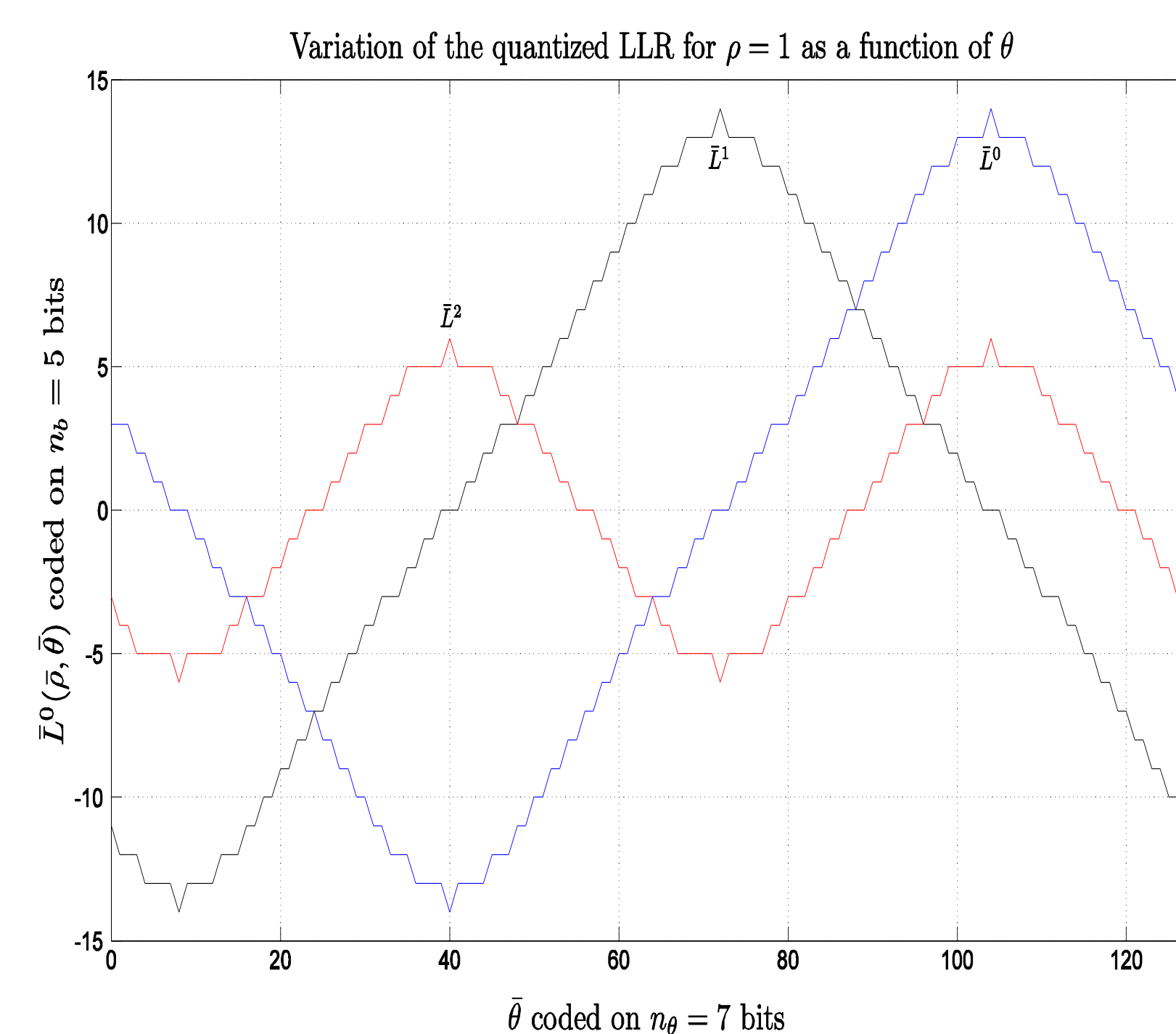


Figure 2 : Quantization of LLR for  $\rho = 1$  as a function of  $\theta$

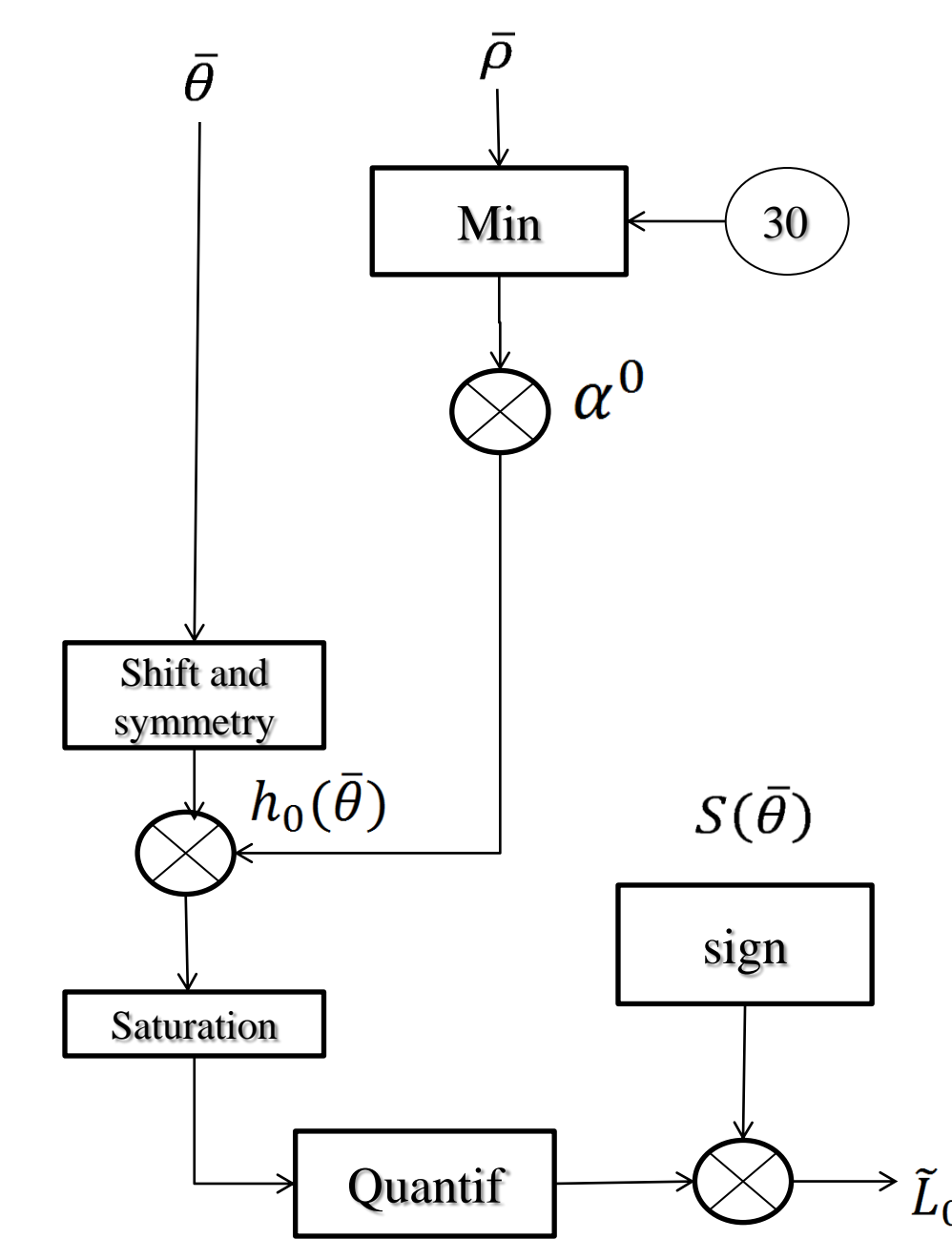


Figure 3 : Architecture of computation of  $\tilde{L}_0$

## CONCLUSIONS

This paper proposes a different approach of two aspects of demapping an 8PSK modulation for DVB-S2 standard. The first one is about using polar coordinates. The preceding step of synchronization can be done in that system of coordinates [2], we thereby save a CORDIC [3] (COordinate Rotation Digital Computer) changing computation. The second aspect concerns the approximation of the LLR using a geometric approach. This method is very simple to implement and allows us to obtain a better reliability than the-state-of-the-art methods.

We can go further by extending the proposed method to the 16-APSK modulation.

## SIMULATION RESULTS

Figure 4 shows the BER as a function of the SNR for a 2/3 and a 3/4 LDPC code rate (short frames  $N = 16200$  bits). The performance is only reduced by 0.02 dB compared to the optimal LLR computation. Table 1 shows that compared to state of art's methods, the proposed linear approximation offers an interesting compromise between the simplicity and the performances.

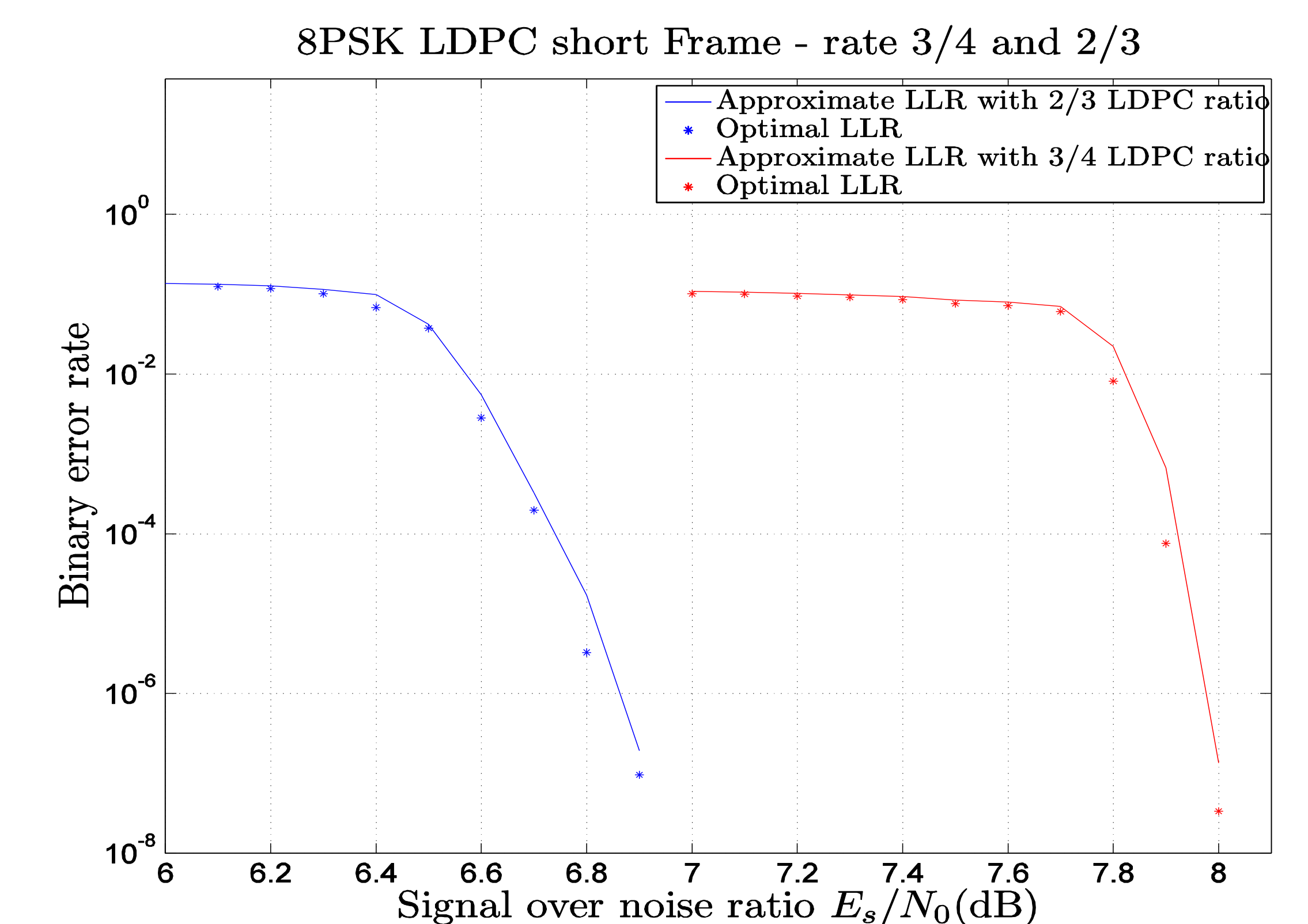


Figure 4 : Error rate as a function of the signal to noise ratio for LDPC rate 2/3 and 3/4

Method	Max [4]	Re-injection of I and Q [5]	Proposed
Required multipliers	16	4	5
MSE	0.94	1.54	0.89

Table 1 : Number of multipliers required to implement different methods of approximation and Mean Square Error (MSE) between approximated LLR and exact quantified LLR.

## REFERENCES

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